

(e) From the above exercises, you can observe that the arithmetic for the transformations seems backwards (especially when compared with the vertical transformations). In this exercise, we are going to explore *why* this is the case.

(i) Consider $g(x) = f(x - 5)$. Write out what $g(2)$ is.

i. Notice that 2 is the input of $g(x)$, not $f(x)$. What is the input of $f(x)$ when 2 is the input of $g(x)$?

- *Note: here, we have transformed backwards (we went from an input of $g(x)$ to an input of $f(x)$).*

ii. Now let 2 be an input of $f(x)$. What is the input of $g(x)$ when 2 is the input of $f(x)$?

- *Note: here, we have transformed in the usual direction (we went from an input of $f(x)$ to an input of $g(x)$).*

iii. What is the input of $g(x)$ when 3 is the input of $f(x)$? What is the input of $g(x)$ when 4 is the input of $f(x)$? In general, what is the input of $g(x)$ when x_0 is *any* input of $f(x)$?

We should now have an idea as to why the arithmetic for the transformations seems backwards. The answer lies in who the x -value being transformed belongs to (i.e. which function's domain is it in?), and who the x -value in the algebraic expression of the function notation belongs to.